Hybrid Music Recommendation using K-Means Clustering

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Abstract

With the expanding digital music industry, the need for good music recommendation systems is becoming more and more relevant. Popular methods such as Collaborative Filtering have been around for a while, and are used extensively. However, the method of Collaborative Filtering is extremely slow. To tackle this, we aim to use K-Means clustering on the user-features modelled using the user's listering history and MFCC features of the songs, in order to reduce the scope of similarity, and run collaborative filtering for a user only on the cluster he belongs to. This method does not limit the scope of the suggestions, while also providing speed to CF. Another problem with CF is that it is based purely on exploitation, and not on exploration. Hence we provide a simple strategy to provide recommendations based on pure exploration.

1 Introduction

The concept of recommendation systems is perhaps the most upfront application of machine learning. With the digital market comprising of over 50% of the recording industry, the problem of Music Recommendation Systems (MRS) has become more relevant over the years.

MRS is of great help for music fans making it easier for them to explore wide collection of songs from a huge ground of versatility and that too based on his taste and preferences. Almost all streaming services such as Apple Music, Spotify, Google Play Music, etc. use recommendation systems to provide new song recommendations to their users.

1.1 Problem Statement

In a typical recommendation system, there is a set of users, and a set of items. Each user rates a subet of items. The task of the recommendation system is to recommend a user u a list of items \mathcal{I} , sorted with the order of relevance to the user. We have a similar goal.

For a given user u, we need to provide at most N suggestions most relevant to his previous listening history. The relevance of the suggestions is measured using truncated mAP (mean Average Precision).

1.2 Motivation

Most of the current MRS use collaborative filtering (CF), which is based on the idea of providing recommendations based on the responses of other users on a given song. Though this approach is evidently very successful and accurate on huge databases of user responses, however it suffers from three major problems Speed, Sparsity and Scalability.

The idea of computing similarity between each user becomes inefficient for recommendation purposes, if there are a large number of users. This calls for a simple and efficient method that sustains the accuracy of CF as well as increase the speed of the recommendations, without much overhead of pre-processing.

As an added side effect, clustering also reduces the sparsity of the user-item ratings (per cluster), which helps in providing more accurate recommendations.

Another caveat of using pure Collaborative Filtering is that the user gets stuck in similar recommendations forever, without enough variation. Henceforth, we try to look on another approach to provide variations in the recommendations provided to the user.

2 Related Work

There are many studies which explore the patterns in the user-item ratings in order to cluster the users or items, effectively reducing the dataset as described earlier.

Ungar et al [1] used Repeated Clustering and Gibbs Sampling directly on the Ratings Matrix to cluster users based on the user's rating history and cluster items based on the users who have rated the corresponding item.

H. Chen and L. Chen [2] proposed Content Based filtering on the user's history, to compute the user's interest in different group of items. For clustering the items, they used inherent features of the MIDI songs.

Dong Kim et al [3] computed the user's interest based on their proposed Dynamic K-Means Clustering. They used STFT (Shortes Time Fourier Transform) features of songs, and infer the user's interest based on the user's history.

There are other studies which use demographic or latent user features for clustering.

Yoshii et al propsed a hybrid solution to collaborative filtering using latent user features. They used a "bag of timbres" to cluster items, and used these to model the users. *Kim et al* used users' demographic features to cluster the users, and then used Collaborative Filtering on the group's rating matrix as well as individual rating's matrix and provided weighted recommendations based on the two approaches.

We propose a combination of the above two approaches, except that we cluster the users based on features modelled using a "bag of songs" approach, and use Collaborative Filtering for a user using only the cluster that the user belongs to as the neighbourhood.

Along with this, we also propose a simple exploration approach to provide recommendations. Since most recommendation strategies in use are based on exploitation, the user generally gets trapped in a bubble, without much variation. Henceforth, we propse a hybrid of exploration and exploitation techniques. In the following section, we discuss the standard method of Collaborative Filtering, and then later, we explain our proposed solution to tackle the three problems of Collaborative Filtering.

3 Collaborative Filtering

Collaborative Filtering is used in almost all commercial recommendor systems. It is based on the simple idea of providing recommendations based on the rating history of similar users. There are two approaches to collaborative filtering.

3.1 Model Based

Model-based recommendation systems involve building a model based on the dataset of ratings. In other words, we extract some information from the dataset, and use that as a "model" to make recommendations without having to use the complete dataset every time. [4]

There are many model-based CF algorithms such as Bayesian networks, clustering models, latent semantic models, etc. Most commonly, dimensionality reduction is used.

We represent the user-item relation as a ratings matrix R where R_{ij} represents the rating that user i has submitted for item j. Also, the $R_{ij} = 0$ if the user i has not used / rated the item j. This allows us to cast the

problem as a low-rank matrix factorization. The user and item features thus obtained can be used to predict the remaining values of ratings matrix.

Model based CF can provide recommendations fast, however it is very difficult to add users or items in this method. This makes the method practically inefficient. Also, the ratings matrix being too sparse causes the method to be inaccurate.

3.2 Memory Based

In this method, we directly use the ratings data to provide suggestions / recommendations. In user-based approach, we compute the similarity between different users and the predicted rating for an item is computed as the aggregation of the ratings for the same item given by similar users. Correspondingly, there is an item-based approach as well.

Similar to the case of model-based, we have a ratings matrix, and the set of unrated entries have the value 0. The most common measure to compute the user-user similarity is the Cosine Similarity Function

$$\texttt{similarity}\left(u_p, u_q\right) = \frac{\sum_{j} R_{pj} \cdot R_{qj}}{\|\mathbf{R}_p\|_2^2 \; \|\mathbf{R}_q\|_2^2}$$

The most common formula for rating aggregation is the weighted sum of the ratings with the weights as the user-user similarity

$$\overline{R_{pj}} = K \sum_i ext{ similarity} \left(u_p, u_i
ight) \cdot R_{ij}$$

The main advantage of memory-based methods is that we can add users and items without any extra hassle, which is not the case with model-based CF. However, computing user-user similarity between all the users is extremely slow, therefore, it becomes a necessity to reduce the dataset. For this, we propose clustering users, and computing the similarity only between uses of the same cluster. We use the same similarity metric as well as the rating aggregation formula.

3.2.1 Locality of the Scoring Function

We can exploit the locality of our similarity function, and add a more generalized version of the scoring as suggested by *Aoilli* [5]. Hence, our new similarity metric becomes the Cosine Similarity powered to *c*.

$$\texttt{similarity}\left(u_{p}, u_{q}\right) = \left(\frac{\sum_{j} R_{pj} \cdot R_{qj}}{\left\|\mathbf{R}_{p}\right\|_{2}^{2} \left\|\mathbf{R}_{q}\right\|_{2}^{2}}\right)^{c}$$

4 Methodology

Our approach to providing suggestions is based on four steps

- 1. Cluster songs using extracted MFCC features
- 2. Model user features based on their listening history and cluster probabilities of the songs
- 3. Cluster users based on their modelled features
- 4. Use User-Based Memory Collaborative Filtering to provide relevant suggestions.

We also propose a simple approach to provide suggestion based purely on exploration, which can be used together with CF based approach to provide mixed recommendations.

4.1 Clustering songs using MFCC features

MFCC (Mel-Frequency Cepstral Coefficients) features have been popularly used in genre classification [6]. MFCC features approximate the human auditory system's response to signals. [7] The features are computed over a window of signals. We refer to this window as timbres.

In order to compute the item features, we find the mean and the standard deviation of each MFCC features of all the timbres of that song. We use these to cluster songs using Soft K-Means Algorithm, with a diagonal covariance matrix.

4.2 Computing User Features

Since we are using Soft K-Means to cluster songs, for each song, we have the cluster weights *i.e.* a vector of length k with each element as probability of that song belonging to the k^{th} cluster. Using these as features vectors, for each user i, we can aggregate this over the songs the i^{th} user has listened to. This serves as a soft "bag of songs" for each user, and hence the user's features.

Let the cluster probabilities for song j be represented by γ^j and the set of songs user i has listened to be represented by \mathcal{I}^i , then we represent the user features for the i^{th} user (\mathbf{u}^i) as

$$\mathbf{u}^i \quad = \quad rac{1}{|\mathcal{I}^i|} \sum_{j \in \mathcal{I}^i} oldsymbol{\gamma}^j$$

Each index l of \mathbf{u}^i represents the inclination of the user i towards the cluster l of the songs. We use these features to further cluster the users, before we finally perform CF.

4.3 Clustering Users

We have the user features modelled as explained in the previous section. We use these to cluster the users, using Soft K-Means with diagonal covariance matrix. We use EM algorithm to solve this, with the latent variables as the cluster assignment.

4.4 **Providing Recommendations**

As mentioned earlier, we provide recommendations using both exploitation as well as exploration. For the exploitation part, we use Collaborative Filtering on clustered users, whereas for the exploitation, we use songs' clusters to provide recommendations from different clusters.

4.4.1 Exploitaion

As explained in Section 2.2, we use memory based collaborative filtering on the user clusters, and rank the suggestions based on their predicted rating. This can also be seen that the similarity between users who belong to different clusters is inherently 0. Therefore, we can rewrite the similarity metric from Section 2.2

$$\texttt{similarity}\left(u_p, u_q\right) = \begin{cases} \frac{\sum_j R_{pj} \cdot R_{qj}}{\|\mathbf{R}_p\|_2^2 \|\mathbf{R}_q\|_2^2} & \texttt{cluster}\left(u^p\right) = \texttt{cluster}\left(u^q\right) \\ 0 & \texttt{else} \end{cases}$$

Using this metric, we need not differentiate on the ranking aggregation or the sorting of the recommendations. Therefore, we find the estimated ratings for each user-song pair, and for each user, report the top songs (at most N) which have non-zero predicted rating.

4.4.2 Exploration

The main idea of exploration is to allow variations in the suggestions provided to the user. The quite popular method Multi Armed Bandits allows providing mixed recommendations for both exploration and exploitation, however, it utilizes the repurchase value of items. Since in providing music recommendations, there must be no song that is repeated, we cannot directly use the method. Also, since our aim is to provide pure exploration, we use a different approach.

As opposed to Multi-Armed Bandits, instead of choosing one song, for each user, we first sample a cluster (from the clusters of the songs) and then provide a single recommendation from this cluster. The sampling of clusters is done using a multinoulli, with the mixinf proportions for the l^{th} cluster given as follows

$$\mathbb{P}\left[z^{i}=l\right] = \frac{1}{K} \sqrt{\frac{|S^{l}|}{\sum_{j \in \Omega^{i} \cap S^{l}} R_{ij}^{-1}}}$$

Here, S^l represents the set of songs in the cluster l and Ω^i represents the set of songs user i has listened to. K is the normalization factor.

These cluster proportions weigh the clusters which user has not extensively explored and weighs down the clusters for which the user has provided lower ratings.

After sampling a cluster, we sort the songs for that cluster in the descending order of their popularity multiplied by the cluster weight. The popularity of a song is essentially the sum of ratings that all users have given for that song. We recommend the top song which the user has not yet listened to.

$$r_{j,l} = \sum_{i} R_{ij} \times \mathbb{P}\left[cluster(j) = l \right]$$

This allows us to present songs which are more popular, and which better represent the clusters which we have sampled.

We can provide k recommendations based on exploration by iterating this process.

We can provide suggestions based on exploitation and exploration in 4-1 ratio, *i.e.* For every 4 songs recommended using exploitation, we recommend 1 song based on exploration.

5 Experiments and Results

5.1 Dataset

We have used the Taste Profile Subset (a subset of the MSD Dataset [8]) which was previously used in the famous MSD Challenge by Kaggle [9]. This dataset provides a list of user-song-count triplets for 1.1 million unique users and 1 million unique songs.

We got the MFCC features for all the songs from MSD Benchmarks provided by Information Management and Preservation [10]. They have provided means and standard deviations for all dimensions of the extracted MFCCs from timbres. The extracted MFCCs are 13 dimensional, and hence the dimensions for song features obtained is 26.

5.1.1 Pre-processing

The following table tells us that the dataset is highly sparse, and thus very prone to overfitting.

Count	Minimum	Maximum	Mean	Median
Users per Song	1	110479	125.794	13
Songs per User	10	4400	47.457	27

For the purpose of training, we have removed users who have listened to lesser than 50 songs. After this step, we were left with approximately 300,000 users.

Also, we have replaced count with a binary value, 1 iff the user has listened to the song. Since the count doesn't necessarily represent the rating of a song, we ignore it, and set $R_{ij} = 1$ iff user *i* has listened to the song *j* at least once.

5.1.2 Train-Evaluation Split

We split the dataset into training and evaluation set based on the users in a 9:1 ratio, *i.e.* 90% of users were considered into the training set, and 10% of the users were considered in the evaluation dataset. The split is made after shuffling the users.

5.2 Number of Clusters for Songs

For the purpose of choosing the number of clustering, we used K-Means algorithm with diagonal covariance matrix over 500 iterations, used the elbow method to determine the optimal number of clusters.

Using the elbow method, we can infer that the optimal number of clusters for songs is $k_s = 10$.

5.3 Number of Clusters for Users

Similar to the previous section, we used K-Means algorithm with diagonal covariance matrix over 500 iterations, and then used the elbow method to determine the optimal number of clusters for the users.

Using the elbow method, we can infer that the optimal number of clusters for users is $k_u = 20$.



Figure 1: K-Means Variance Plot for Songs Clustering



Tracks MFCC: LDA Plot (After GMM)

Figure 2: LDA Plot of Track Features after GMM on 10 clusters

5.4 Recommendations based on Exploitation

After clustering users, we use Collaborative Filtering on all clusters independently, as explained in section 4.4.1. Since A/B testing is not possible, we use truncated mAP@N (Mean Average Precision) to compare accuracies for different localization exponents.

Users Clustering: Inertia for K-Means



Figure 3: K-Means Variance Plot for Users Clustering



User Features: LDA Plot (After GMM)

Figure 4: LDA Plot of User Features after GMM on 20 clusters

5.4.1 Truncated Mean Average Precision

In the case of recommendations, without A/B testing, it is difficult to correctly estimate the accuracy of a recommendor system. Since we cannot put a negative score on any recommendation, as we do not know the user's opinions on that tracks, it makes sense to consider only the precision.

mAP is a very popular metric in estimating the accuracy of a recommendor system. It was also used in the MSD dataset as the evaluation metric. It is essentially the mean of the average precision for every user.

For every user i, first the average precision is calculated as the average of the Precision@k for every recall point *i.e.* for every suggestion ranked at k that the user has listened to, we take the precision over the first k recommendations and we compute the average over all such k's. To calculate the mAP, simply average over the average precisions for all users.

From the following table, we can infer that for user-user similarity, the optimal localization exponent is 7, as it provides the highes mAP@500.

Localization Exponent (c)	mAP@500	
1	0.153092110732	
2	0.206804120034	
3	0.24325832841	
4	0.262761192183	
5	0.272772400673	
6	0.27679672424	
7	0.278189125154	
8	0.277665534322	
9	0.276124011391	

If we compare the value with the highest mAP obtained by the winner of the MSD Challenge, who got the best mAP@500 value equal to 0.17144, we have a significantly higher computed mAP. Although this is not a proper benchmark as the evaluation set is different, however, we can still infer that our model is good, and compares well to other recommedor systems.

We also show the suggestions generated for the first use r in our evaluation set in the plot in Figure 5. The suggestions are generated with the localization exponent c = 7. The blue points represent the songs that the users has listened to, whereas the black points represent the songs recommended to the user.

We can see that the recommendations are close enough to the actual tracks the user has listened to, and hence can conclude the suggestions might be relevant.

5.5 Recommendations based on Exploration

Since exploration is purely based on A/B testing, we cannot have any benchmark test for this factor. We show the explored recommendations for the first user in our evaluation set in the plot (Figure 6). Similar to the exploitation case, the blue points represent the songs that the user has listened to, whereas the black points represent the songs recommended to the user.

It can be observed that the recommendations based on exploration are quite random, as well as very dissimilar to the songs already listened to by the user. Therefore, we can conclude that the suggestions provided from our approach satisfy the necessities of pure exploration based recommendor system.

Tracks MFCC: LDA Plot (After GMM)



Figure 5: Recommendations based on Exploitation to a User (c = 7)



Tracks MFCC: LDA Plot (After GMM)

Figure 6: Recommendations based on Exploration to a User

6 Conclusion

From the results, we can conclude that our exploitation approach provides good and relevant suggestions, and comparable to existing approaches to Collaborative Filtering, wheras our exploration strategy provides sufficient amount of variation to the recommendations.

Our results suggests that clustering does not have a major effect on the quality of recommendations, while reducing the time taken to generatate predictions by a huge factor. Since GMM and K-Means are fast algorithms, we have also ensured that the overhead of pre-processing is not very huge. Also, adding new users and songs is easy since we need not recompute the clusters very often, moreover, since we are using Memory-Based Collaborative Filtering which can easily handle additional users and tracks, without much recompution overhead.

7 Future Work

We can change the User-User Similarity metric to Localized Adjusted Cosine Similarty [5] for better and more accurate recommendations. Also, we can use item-based collaborative filtering, which has been shown to be have better results [5] and is considered more stable.

When the number of users increase, say over 100 millions (such as the case for Spotify [11]), we can try landmarking the users, based on the number of items they have rated and their cluster weights, and provide recommendations considering only those users. Another approach could be to user hierarchical clustering, and collapsing inner-clusters into a group, and converting the items set to be a bag of items from all the users in the group.

In order to tackle the cold-start problem of Collaborative Filtering, we can try providing weighted suggestions based on artist-artist similarity, and other demographic features of the user [12]. We can also expand the concept of exploration to artists, and explore on artists rather that tracks' clusters.

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